

WORKING PAPER

 N° 2022-4

ENDOGENOUS TIMING OF TECHNOLOGICAL CHOICES OF FLEXIBILITY IN A MIXED DUOPOLY

ARMEL JACQUES

www.tepp.eu

TEPP – Theory and Evaluation of Public Policies - FR CNRS 2042

Endogenous timing of technological choices of flexibility in a mixed duopoly

Armel JACQUES*

March 10, 2022

Abstract

We study the adoption choices of flexible technologies to increase the range of products in a mixed duopoly. When firms' technological choices are simultaneous, the public ownership of a firm increases its incentives to adopt flexible technology and reduces those of its private competitor. The technologies used by the two firms can be reversed if the private firm chooses its technology before the public firm. If we make the timing of technological choices endogenous, it is simultaneous choices that are the equilibrium.

Keywords: Mixed duopoly, flexibility, technological choices, endogenous timing.

JEL Classification numbers: L32, L33, L13, O33.

^{*}CEMOI TEPP-CNRS (FR2042), Université de La Réunion, Faculté de Droit et d'Economie, 15, avenue René Cassin, 97715 Saint-Denis messag cedex 9. Email : Armel.Jacques@univ-reunion.fr.

1 Introduction

In recent decades, many firms have replaced their traditional production lines with more robotic and flexible facilities. These flexible systems make it possible to adjust the pace of production more quickly to change in demand and to extend the range of goods that can be produced on the same production line.¹ In this study, we will focus on this second aspect.²

Röller and Tombak (1990) [RT continued] were among the first to develop a model designed to study the determinants of the adoption of flexible technology to extend the range of goods produced in a strategic context. Their study was extended by Röller and Tombak (1993), who increased the number of firms, Boyer, Jacques and Moreaux (2000), who analysed the impact of the possibilities of observing or not observing the technological choices of the competing firm before deciding on production levels, Jacques (2006 and 2021), who introduced the possibility for firms to enter into collusion agreements, and Bárcena-Ruiz and Olaizola (2008), who assumed that firm choices could be delegated to managers to whom they were able to strategically assign a different objective from profit maximization.

Previous studies have limited themselves to oligopolies consisting solely of private firms. Gil-Moltó and Poyago-Theotoky (2008) [GMPT thereafter] have pointed out that public firms, or firms in which public authorities hold significant holdings, are present in many industries,³ especially in Europe and Asia. To analyse the impact of the public ownership of one of the firms on the adoption of flexible technologies, they have developed a model of choice of flexibility in a mixed duopoly, based on RT's model. As in most articles on mixed oligopolies, the authors assumed that the private firm was trying to maximise its profits while the public firm was trying to maximise the social surplus. The authors have therefore adopted as the objective of the public firm the social surplus function given by RT. Unfortunately, the latter contains an error due to the omission of a term in the consumer surplus.⁴ The correction of this error significantly changes the results obtained by GMPT.

GMPT limited themselves to the study of technological choices when the firms make this choice simultaneously. However, the literature on mixed oligopolies has shown that the results obtained in this type of oligopoly often depend on the order of choice of the firms. In addition, the contributions which have endeavoured to make the timing of choices endogenous have led to rather contrasting results, but have shown the importance of not neglecting cases where the firm's choices are sequential. Sequential timings seem more likely when firms compete in quantities (Pal, 1998; Matsumura, 2003a; Jacques, 2004; Lu, 2006; Matsumura and Ogawa, 2010) and when they compete through R&D investments (Zikos, 2007). On the other hand, the chronology with simultaneous choices emerges when firms compete in price (Bárcena-Ruiz, 2007; Méndez-Naya, 2015). In other contexts, the timing of the equilibrium depends on the parameter values. This is the

¹See Jacques (2003) for a survey.

²On the first aspect, see notably Boyer and Moreaux (1997) and Boyer, Jacques and Moreaux (2002).

³See GMPT for examples.

⁴See Castanheira de Moura and Jacques (2002).

case when firms compete in quantities with uncertainty about the level of demand that is resolved over time (Anam, Basher and Chiang, 2007) or when firms have to choose locations, and then start wage negotiations with their employees (Bárcena-Ruiz and Casado-Izaga, 2012). Finally, some models allow several types of timing as equilibria (Matsumura, 2003b) or may not admit pure strategies equilibrium (Zhang and Li, 2013). It therefore seems interesting to ask how the technological choices of firms are impacted by a change in chronology and to look for the timing that seems most likely if firms can influence it.

In this study, we extend the work of GMPT by analysing the technological choices of firms when they make their choice of flexibility sequentially and by determining the equilibrium timing when firms can decide when they make their choice of technology. This objective requires prior to resuming the case where the choices are simultaneous to eliminate the errors related to a mistake in the expression of the consumer surplus used by RT and GMPT.

In the mixed duopoly, when firms simultaneously choose their technology, they opt for flexible technology if the additional cost of the latter compared to a dedicated technology is low. Both firms adopt dedicated technologies if the additional cost of flexibility is high. If the additional cost of flexible technology lies between these two extremes, the equilibrium technological configuration is asymmetrical. The state-owned firm chooses flexible technology and the private company chooses a dedicated technology. The reverse technological configuration never appears in equilibrium. The area where the technological configuration is asymmetrical in the mixed duopoly totally encompasses the area where it is also asymmetrical in a duopoly composed of two private firms. The public firm therefore has more incentives than a private firm to adopt flexible technology and expand its product range. The intuition behind this result is that flexible technology makes competition more intense and increases consumer surplus. The public firm incorporates this beneficial impact for consumers, which leads it to choose flexibility for a wider range of parameter values than a private firm. In contrast, a private firm has less incentive to acquire flexible technology if it is opposed to a public firm than if it is confronted with another private firm. Indeed, taking into account the consumer surplus encourages a public firm to produce more than a private firm would. In reaction, its private competitor produces less than if it were confronted with a private firm. It therefore has less incentive to invest in expanding its product range.

If the public company selects its technology before the private company, the equilibrium technological configurations remain identical to those obtained in the game with simultaneous choices. The state-owned firm could use its leadership position to set up different configurations, but it never has any interest in doing so. On the other hand, if the role of leader is assigned to the private firm, the latter uses it, for certain parameter values, to implement an asymmetrical technological configuration in which it exploits a flexible technology while the public company uses a dedicated technology. The modification of the chronology of the game can therefore lead to an inversion of the tehnologies used by the two firms. When firms can decide when they will make the choice of their technology, everyone wants to make that choice as soon as possible to take on the leadership role. As a result, in equilibrium, the timing that imposes itself on equilibrium is

that in which the technological choices of firms are simultaneous.

When the ownership of firms has no impact on the equilibrium technological configuration, the social surplus is always higher in the mixed duopoly than in the private duopoly. It is therefore not in the interest of public authorities to privatise the public firm in these ranges of parameter values. On the other hand, when the privatization of the state-owned firm prompts its competitor to change technology in order to adopt flexible technology, this privatization sometimes increases the social surplus. When the private firm is the leader in the mixed duopoly, privatization of the public firm is desirable when the technological configuration is asymmetrical and the flexible technology is exploited by the private firm.

The model assumptions are presented in the next section. Section 3 analyses the case where the technological choices of the two firms are simultaneous. In section 4, we study the impact of a modification of the game's chronology on equilibrium technological configurations. In section 5, we make the timing of the game endogenous. In section 6, we determine the cases where privatization of the public firm increases the social surplus.

2 Model

We take the hypotheses of the model of Gil-Moltó and Poyago-Theotoky (2008) [GMPT in the following], which is itself based on that of Röller and Tombak (1990) [RT thereafter].

The model includes two firms (1 and 2), two goods (A and B) and two technologies: flexible (F) and dedicated (D). Flexible technology makes it possible to produce both goods. A dedicated technology makes it possible to produce only one. If firm 1 opts for dedicated technology, it produces good A while if firm 2 selects dedicated technology, it produces good B. The fixed cost of dedicated technology is equal to $F_D = 1$. Flexible technology fixed cost is higher, but lower than the cost of acquiring two dedicated technologies: $F_F = 1 + s$, with $s \in [0, 1[$.

Firms' variable costs are quadratic:⁵

$$C\left(q_{i}^{A}, q_{i}^{B}\right) = \left(q_{i}^{A}\right)^{2} + \left(q_{i}^{B}\right)^{2}$$

The model is divided into two stages. In the first stage, the two firms choose their technology simultaneously. In the second case, they compete in quantities \dot{a} la Cournot, having observed the technology chosen by the competing firm. In Section 4, the timeline of the game will be modified and cases where firms make their technological choices sequentially will be investigated.

RT only deal with the case where the two firms are private firms, whose objective is to maximise profit.

 $^{^{5}}$ This functional form is the one chosen by GMPT. RT assume that the marginal cost of firms is constant and identical for both technologies. However, with the latter hypothesis, the production of the private firm may be zero in a mixed duopoly if the public firm produces the same good at the same cost. To overcome this problem, GMPT introduced quadratic production costs.

GMPT also analyze the case where firm 1 is private while firm 2 is state-owned. In this mixed duopoly, the authors assume that the objective of the private firm is to maximise its profit while that assigned to the public firm is to maximise the welfare.

The demand for both goods comes from a representative consumer whose utility function is:

$$U(Q^{A}, Q^{B}) = a(Q^{A} + Q^{B}) - \frac{1}{2}\left[(Q^{A})^{2} + (Q^{B})^{2} + 2\lambda Q^{A}Q^{B}\right] + I$$

where I is the quantity consumed of a composite good. $\lambda \in [0, 1]$ measures the degree of substitutability between the two goods.

From this utility function, we can deduce the inverse demand functions for goods A and B:

$$p^{A} \left(Q^{A}, Q^{B} \right) = a - Q^{A} - \lambda Q^{B}$$
$$p^{B} \left(Q^{A}, Q^{B} \right) = a - Q^{B} - \lambda Q^{A}$$

as well as the consumer surplus:

$$CS(Q^{A}, Q^{B}) = U(Q^{A}, Q^{B}) - p^{A}Q^{A} - p^{B}Q^{B} = \frac{1}{2}\left[\left(Q^{A}\right)^{2} + \left(Q^{B}\right)^{2}\right] + \lambda Q^{A}Q^{B}$$

RT argue (page 424) that the consumer surplus is equal to $\frac{1}{2}\left[\left(Q^A\right)^2 + \left(Q^B\right)^2\right]$, which is inconsistent with the presented utility function (page 420).⁶ This error spread to GMPT, which used the RT formula.

The error also spread to the calculation of the total surplus, since the consumer surplus is one of the components of the social surplus:

$$TS = \pi_1 + \pi_2 + CS$$

However, maximization of this function is the objective assigned to the public firm in the mixed duopoly. The error in the consumer surplus formula therefore affects a significant portion of GMPT's results.⁷

3 Simultaneous technological choices

The case where technological choices are simultaneous has already been dealt with by GMPT, however when changing the formula of consumer surplus, many results change. The results presented in this section are therefore very different from those presented by GMPT.

We're looking for the perfect Nash equilibria of the model. We start by solving the quantities competition stage for each of the possible technological configurations before determining the technological choices of the firms.

⁶As mentioned by Castanheira de Moura and Jacques (2002) and Jacques (2003).

 $^{^{7}\}mathrm{In}$ particular lemmas 4, 5 and 6 and propositions 2, 3 and 4.

3.1 Cournot competition

We first present the results obtained in a private duopoly before presenting those corresponding to a mixed duopoly.

3.1.1 Private duopoly

In the second stage, firms compete in quantities. Since the calculations are relatively standard, we limit ourselves, in the body of the text, to indicating the results obtained for each of the technological configurations (the first [second] letter, in the first column, indicates the technology of which the firm 1 [2] is equipped). The process that led to these results is a little more detailed in the appendix.

	Quantities	Prices	Payoffs
D,D	$q_1^A = \frac{1}{4+\lambda}a$ $q_2^A = 0$ $q_1^B = 0$ $q_2^B = \frac{1}{4+\lambda}a$	$p^{A} = \frac{3}{4+\lambda}a$ $p^{B} = \frac{3}{4+\lambda}a$	$\pi_{1} = \frac{2}{(4+\lambda)^{2}}a^{2} - F_{D}$ $\pi_{2} = \frac{2}{(4+\lambda)^{2}}a^{2} - F_{D}$ $CS = \frac{1+\lambda}{(4+\lambda)^{2}}a^{2}$ $TS = \frac{5+\lambda}{(4+\lambda)^{2}}a^{2} - 2F_{D}$
F,F	$q_1^A = \frac{1}{5+3\lambda}a$ $q_2^A = \frac{1}{5+3\lambda}a$ $q_1^B = \frac{1}{5+3\lambda}a$ $q_2^B = \frac{1}{5+3\lambda}a$	$p^{A} = \frac{3+\lambda}{5+3\lambda}a$ $p^{B} = \frac{3+\lambda}{5+3\lambda}a$	$\pi_1 = \frac{2(2+\lambda)}{(5+3\lambda)^2}a^2 - F_F$ $\pi_2 = \frac{2(2+\lambda)}{(5+3\lambda)^2}a^2 - F_F$ $CS = \frac{4(1+\lambda)}{(5+3\lambda)^2}a^2$ $TS = \frac{4(3+2\lambda)}{(5+3\lambda)^2}a^2 - 2F_F$
F,D	$\begin{array}{l} q_1^A = \frac{3(5-3\lambda)}{4(15-4\lambda^2)}a \\ q_2^A = 0 \\ q_1^B = \frac{12-7\lambda+\lambda^2}{4(15-4\lambda^2)}a \\ q_2^B = \frac{6-\lambda-\lambda^2}{2(15-4\lambda^2)}a \end{array}$	$p^{A} = \frac{45 - 15\lambda - 7\lambda^{2} + \lambda^{3}}{4(15 - 4\lambda^{2})}a$ $p^{B} = \frac{3(6 - \lambda - \lambda^{2})}{2(15 - 4\lambda^{2})}a$	$\pi_{1} = \frac{369 - 258\lambda - 59\lambda^{2} + 64\lambda^{3} - 8\lambda^{4}}{8(15 - 4\lambda^{2})^{2}}a^{2} - F_{F}$ $\pi_{2} = \frac{(6 - \lambda - \lambda^{2})^{2}}{2(15 - 4\lambda^{2})^{2}}a^{2} - F_{D}$ $CS = \frac{801 + 18\lambda - 588\lambda^{2} + 150\lambda^{3} + 19\lambda^{4}}{32(15 - 4\lambda^{2})^{2}}a^{2}$ $TS = \frac{2853 - 1206\lambda - 1000\lambda^{2} + 438\lambda^{3} + 3\lambda^{4}}{32(15 - 4\lambda^{2})^{2}}a^{2} - F_{D} - F_{F}$
D,F	$\begin{array}{c} q_1^A = \frac{6 - \lambda - \lambda^2}{2(15 - 4\lambda^2)} a \\ q_2^A = \frac{12 - 7\lambda + \lambda^2}{4(15 - 4\lambda^2)} a \\ q_1^B = 0 \\ q_2^B = \frac{3(5 - 3\lambda)}{4(15 - 4\lambda^2)} a \end{array}$	$p^{A} = \frac{3(6-\lambda-\lambda^{2})}{2(15-4\lambda^{2})}a$ $p^{B} = \frac{45-15\lambda-7\lambda^{2}+\lambda^{3}}{4(15-4\lambda^{2})}a$	$\pi_{1} = \frac{\left(6 - \lambda - \lambda^{2}\right)^{2}}{2(15 - 4\lambda^{2})^{2}}a^{2} - F_{D}$ $\pi_{2} = \frac{369 - 258\lambda - 59\lambda^{2} + 64\lambda^{3} - 8\lambda^{4}}{8(15 - 4\lambda^{2})^{2}}a^{2} - F_{F}$ $CS = \frac{801 + 18\lambda - 588\lambda^{2} + 150\lambda^{3} + 19\lambda^{4}}{32(15 - 4\lambda^{2})^{2}}a^{2}$ $TS = \frac{2853 - 1206\lambda - 1000\lambda^{2} + 438\lambda^{3} + 3\lambda^{4}}{32(15 - 4\lambda^{2})^{2}}a^{2} - F_{D} - F_{F}$

3.1.2 Mixed duopoly

As for the private duopoly, we limit ourselves to giving the results and we refer to the appendix for the presentation of the details of the approach.

	Quantities	Prices	Payoffs
D,D	$q_1^A = \frac{3-\lambda}{12-\lambda^2}a$ $q_2^A = 0$ $q_1^B = 0$ $q_2^B = \frac{4-\lambda}{12-\lambda^2}a$	$p^{A} = \frac{9-3\lambda}{12-\lambda^{2}}a$ $p^{B} = \frac{8-2\lambda}{12-\lambda^{2}}a$	$\pi_{1} = \frac{2(3-\lambda)^{2}}{(12-\lambda^{2})^{2}}a^{2} - F_{D}$ $\pi_{2} = \frac{(4-\lambda)^{2}}{(12-\lambda^{2})^{2}}a^{2} - F_{D}$ $CS = \frac{25+10\lambda-12\lambda^{2}+2\lambda^{3}}{2(12-\lambda^{2})^{2}}a^{2}$ $TS = \frac{93-30\lambda-6\lambda^{2}+2\lambda^{3}}{2(12-\lambda^{2})^{2}}a^{2} - 2F_{D}$
F,F	$q_1^A = \frac{2}{11+8\lambda+\lambda^2}a$ $q_2^A = \frac{3+\lambda}{11+8\lambda+\lambda^2}a$ $q_1^B = \frac{2}{11+8\lambda+\lambda^2}a$ $q_2^B = \frac{3+\lambda}{11+8\lambda+\lambda^2}a$	$p^{A} = \frac{2(3+\lambda)}{11+8\lambda+\lambda^{2}}\alpha$ $p^{B} = \frac{2(3+\lambda)}{11+8\lambda+\lambda^{2}}\alpha$	$\pi_{1} = \frac{8(2+\lambda)}{(11+8\lambda+\lambda^{2})^{2}}a^{2} - F_{F}$ $\pi_{2} = \frac{2(3+\lambda)^{2}}{(11+8\lambda+\lambda^{2})^{2}}a^{2} - F_{F}$ $CS = \frac{(1+\lambda)(5+\lambda)^{2}}{(11+8\lambda+\lambda^{2})^{2}}a^{2}$ $TS = \frac{59+55\lambda+13\lambda^{2}+\lambda^{3}}{(11+8\lambda+\lambda^{2})^{2}}a^{2} - 2F_{F}$
F,D	$q_1^A = \frac{11 - 7\lambda}{4(11 - 3\lambda^2)} a$ $q_2^A = 0$ $q_1^B = \frac{8 - 5\lambda + \lambda^2}{4(11 - 3\lambda^2)} a$ $q_2^B = \frac{12 - 2\lambda - 2\lambda^2}{4(11 - 3\lambda^2)} a$	$p^{A} = \frac{33 - 13\lambda - 5\lambda^{2} + \lambda^{3}}{4(11 - 3\lambda^{2})}a$ $p^{B} = \frac{6 - \lambda - \lambda^{2}}{11 - 3\lambda^{2}}a$	$\pi_{1} = \frac{370 - 292\lambda - 42\lambda^{2} + 72\lambda^{3} - 12\lambda^{4}}{16(11 - 3\lambda^{2})^{2}}a^{2} - F_{F}$ $\pi_{2} = \frac{\left(12 - 2\lambda - 2\lambda^{2}\right)^{2}}{16(11 - 3\lambda^{2})^{2}}a^{2} - F_{D}$ $CS = \frac{521 + 6\lambda - 376\lambda^{2} + 90\lambda^{3} + 15\lambda^{4}}{32(11 - 3\lambda^{2})^{2}}a^{2}$ $TS = \frac{1549 - 674\lambda - 548\lambda^{2} + 250\lambda^{3} - \lambda^{4}}{32(11 - 3\lambda^{2})^{2}}a^{2} - F_{F} - F_{D}$
D,F	$\begin{array}{l} q_1^A = \frac{2(3-\lambda)}{33-5\lambda^2} a \\ q_2^A = \frac{3(3-\lambda)}{33-5\lambda^2} a \\ q_1^B = 0 \\ q_2^B = \frac{11-5\lambda}{33-5\lambda^2} a \end{array}$	$p^{A} = \frac{6(3-\lambda)}{33-5\lambda^{2}}a$ $p^{B} = \frac{2(11-5\lambda)}{33-5\lambda^{2}}a$	$\pi_{1} = \frac{8(3-\lambda)^{2}}{(33-5\lambda^{2})^{2}}a^{2} - F_{D}$ $\pi_{2} = \frac{2(101-82\lambda+17\lambda^{2})}{(33-5\lambda^{2})^{2}}a^{2} - F_{F}$ $CS = \frac{173+35\lambda-105\lambda^{2}+25\lambda^{3}}{(33-5\lambda^{2})^{2}}a^{2}$ $TS = \frac{447-177\lambda-63\lambda^{2}+25\lambda^{3}}{(33-5\lambda^{2})^{2}}a^{2} - F_{D} - F_{F}$

3.2 Technological choices

After determining the quantities produced in each of the possible technological configurations, we analyze the technological choices of the firms. We start by determining the best response of one firm to the technology chosen by the other firm. We then determine the equilibria of the first stage of the game.

3.2.1 Best reply to the technology chosen by the competing firm

We start with the private duopoly and we continue with the analysis of the mixed duopoly.

Private duopoly: Flexible technology is the best reply to flexible technology if and only if:⁸

$$\pi_1(F,F) \ge \pi_1(D,F) \Leftrightarrow \frac{2(2+\lambda)}{(5+3\lambda)^2} - \frac{\left(6-\lambda-\lambda^2\right)^2}{2\left(15-4\lambda^2\right)^2} \ge \frac{s}{a^2}$$

Flexible technology is the best response to dedicated technology if and only if:

$$\pi_1(F,D) \ge \pi_1(D,D) \Leftrightarrow \frac{369 - 258\lambda - 59\lambda^2 + 64\lambda^3 - 8\lambda^4}{8\left(15 - 4\lambda^2\right)^2} - \frac{2}{\left(4 + \lambda\right)^2} \ge \frac{s}{a^2}$$

These conditions are more easily verified if the additional cost of flexible technology, s, is low and if the potential demand of consumers, a, is high.

⁸The first [second] letter appearing in the profit expressions is the technology chosen by firm 1 [2].

The expressions to the left of these inequalities are decreasing functions of λ . When λ increases, the two goods become closer substitutes. The amount that firms are willing to pay to acquire a technology to produce both goods logically decreases as λ increases.

It may be noted that, even if the two goods become perfect substitutes ($\lambda = 1$), the firms are still willing to pay a strictly positive sum to acquire the possibility of producing the second good. This is because the costs are quadratic. Thus, even if the two goods are identical, acquiring a second production line has a positive value, because it reduces the firm's variable production costs.

Mixed duopoly: The two firms having different objective functions, they have different better replies to the technological choice of the other firm. We start by studying the best replies from the private firm, then we determine those from the state-owned firm.

Best responses from private firm. Flexibility is the best response to the flexibility of the public firm if and only if:

$$\pi_1(F,F) \ge \pi_1(D,F) \Leftrightarrow \frac{8\left(2+\lambda\right)}{\left(11+8\lambda+\lambda^2\right)^2} - \frac{8\left(3-\lambda\right)^2}{\left(33-5\lambda^2\right)^2} \ge \frac{s}{a^2}$$

Adopting flexible technology is the best reply to the choice of a dedicated technology by the public company if and only if:

$$\pi_1(F,D) \ge \pi_1(D,D) \Leftrightarrow \frac{370 - 292\lambda - 42\lambda^2 + 72\lambda^3 - 12\lambda^4}{16(11 - 3\lambda^2)^2} - \frac{2(3-\lambda)^2}{(12-\lambda^2)^2} \ge \frac{s}{a^2}$$

As in the previous case, the expressions to the left of the inequalities are decreasing functions of λ .

Best responses from the public firm. Flexibility is the best response to the adoption of flexible technology by the private firm if and only if:

$$TS\left(F,F\right) \ge TS\left(D,F\right) \Leftrightarrow \frac{59 + 55\lambda + 13\lambda^{2} + \lambda^{3}}{\left(11 + 8\lambda + \lambda^{2}\right)^{2}} - \frac{1549 - 674\lambda - 548\lambda^{2} + 250\lambda^{3} - \lambda^{4}}{32\left(11 - 3\lambda^{2}\right)^{2}} \ge \frac{s^{2}}{a^{2}} + \frac{1549 - 674\lambda - 548\lambda^{2} + 250\lambda^{3} - \lambda^{4}}{32\left(11 - 3\lambda^{2}\right)^{2}} \ge \frac{s^{2}}{a^{2}} + \frac{1549 - 674\lambda - 548\lambda^{2} + 250\lambda^{3} - \lambda^{4}}{32\left(11 - 3\lambda^{2}\right)^{2}} \ge \frac{s^{2}}{a^{2}} + \frac{1549 - 674\lambda - 548\lambda^{2} + 250\lambda^{3} - \lambda^{4}}{32\left(11 - 3\lambda^{2}\right)^{2}} \ge \frac{s^{2}}{a^{2}} + \frac{1549 - 674\lambda - 548\lambda^{2} + 250\lambda^{3} - \lambda^{4}}{32\left(11 - 3\lambda^{2}\right)^{2}} \ge \frac{s^{2}}{a^{2}} + \frac{1549 - 674\lambda - 548\lambda^{2} + 250\lambda^{3} - \lambda^{4}}{32\left(11 - 3\lambda^{2}\right)^{2}} \ge \frac{s^{2}}{a^{2}} + \frac{1549 - 674\lambda - 548\lambda^{2} + 250\lambda^{3} - \lambda^{4}}{32\left(11 - 3\lambda^{2}\right)^{2}} \ge \frac{s^{2}}{a^{2}} + \frac{1549 - 674\lambda - 548\lambda^{2} + 250\lambda^{3} - \lambda^{4}}{32\left(11 - 3\lambda^{2}\right)^{2}} \ge \frac{s^{2}}{a^{2}} + \frac{1549 - 674\lambda - 548\lambda^{2} + 250\lambda^{3} - \lambda^{4}}{32\left(11 - 3\lambda^{2}\right)^{2}} \ge \frac{s^{2}}{a^{2}} + \frac{1549 - 674\lambda - 548\lambda^{2} + 250\lambda^{3} - \lambda^{4}}{32\left(11 - 3\lambda^{2}\right)^{2}} \ge \frac{s^{2}}{a^{2}} + \frac{1549 - 674\lambda - 548\lambda^{2} + 250\lambda^{3} - \lambda^{4}}{32\left(11 - 3\lambda^{2}\right)^{2}} \ge \frac{s^{2}}{a^{2}} + \frac{1549 - 674\lambda - 548\lambda^{2} + 250\lambda^{3} - \lambda^{4}}{32\left(11 - 3\lambda^{2}\right)^{2}} \ge \frac{s^{2}}{a^{2}} + \frac{1549 - 674\lambda - 548\lambda^{2} + 250\lambda^{3} - \lambda^{4}}{32\left(11 - 3\lambda^{2}\right)^{2}} \ge \frac{s^{2}}{a^{2}} + \frac{1549 - 674\lambda - 548\lambda^{2} + 250\lambda^{3} - \lambda^{4}}{32\left(11 - 3\lambda^{2}\right)^{2}} \ge \frac{s^{2}}{a^{2}} + \frac{1549 - 674\lambda - 548\lambda^{2} + 250\lambda^{2}}{32\left(1 - 3\lambda^{2}\right)^{2}} = \frac{1549 - 674\lambda - 548\lambda^{2}}{32\left(1 - 3\lambda^{2}\right)^{2}} = \frac{1540 - 548\lambda^{2}}{32\left(1 - 3\lambda^{2}\right)^{2}}$$

Opting for flexible technology is the best reply to the choice of a dedicated technology by the private company if and only if:

$$TS\left(F,D\right) \ge TS\left(D,D\right) \Leftrightarrow \frac{447 - 177\lambda - 63\lambda^{2} + 25\lambda^{3}}{\left(33 - 5\lambda^{2}\right)^{2}} - \frac{93 - 30\lambda - 6\lambda^{2} + 2\lambda^{3}}{2\left(12 - \lambda^{2}\right)^{2}} \ge \frac{s}{a^{2}}$$

The left members of inequalities are decreasing functions of λ . Like the private firm, the public firm is willing to invest less to acquire flexible technology if the two goods are closer substitutes. GMPT gets a different result for the second condition. They find that this condition is a nonmonotonous function of λ . They get a U-shape. Which seems pretty counterintuitive.

3.2.2 Technological equilibria

We can now determine the equilibria of the first stage of the game.

Graphic representation: We start by showing on the same graph, the six functions of the previous technological best replies. Like Boyer, Jacques and Moreaux (2000), we chose to put $\frac{s}{a^2}$ on the y-axis rather than s. This avoids having to arbitrarily set a value for one of the parameters and allows us to visualize all the results on one graph.

The highest border is the best response from the public firm to D. Moving down, we then have (in dotted lines) the best response from the public firm to F. The next two boundaries correspond to those of a private duopoly. The best reply to D is above the best answer to F. Finally come the best replies of the private firm to the technological choice of the public firm in a mixed duopoly. The highest (dotted) is the best response to D; the lowest is the best response to F. The following figure is thus obtained.





The table below shows the technological equilibrium obtained in each of the five relevant areas of the figure for each of the two types of duopoly.

	Private duopoly	Mixed duopoly
1	(D,D)	(D,D)
2	(D,D)	(D,F)
3	(D,F) or (F,D)	(D,F)
4	(F,F)	(D,F)
5	(F,F)	(F,F)

We can emphasize that the different borders do not cut on this figure. The results obtained are therefore very different from those of GMPT where several intersections of the best technological responses appear.⁹

Private duopoly: The situation where the two firms are private will serve as a point of comparison to understand the impact of the public ownership of one of the firms. It is also of interest in itself. Indeed, this situation has already been studied by RT, but for the case where the firms' cost functions are linear. It is interesting to see if the results are robust to a change in the cost function.¹⁰

The two best reply functions that correspond to those of a private firm versus another private firm are those that delimit zone 3. The most notable result is that the border corresponding to the best response to a flexible technology is above the one corresponding to the best response to a dedicated technology. The position of these two frontiers is therefore reversed in relation to that obtained with a constant marginal cost (Kim, Röller and Tombak, 1992). The results therefore diverge for the intermediate values of s/a^2 . RT get a flexible trap. This is an area where there are two equilibria in pure strategies, (D, D) and (F, F), and in which firms prefer equilibrium (D, D). There is therefore no area where the two firms make different technological choices in a pure strategies equilibrium.¹¹ With quadratic costs, there is a range of values of s/a^2 for which firms adopt different technologies.

Outside the previous zone, we find the RT fund trends. Firms adopt F technology when its fixed cost is low relative to the size of the market and when the differentiation between the two goods is strong. Firms adopt tehnology D in opposite cases.

Mixed duopoly: If the additional fixed cost of flexibility is very low, both firms opt for technology F (zone 5). If the additional cost of flexibility is very high, both firms choose a dedicated technology (zone 1). Between these two cases (zones 2 to 4), firms adopt different technologies. The public firm invests in flexible technology and therefore produces both goods. The private company installs a dedicated technology and is limited to the production of good B.

 $^{^{9}}$ See their figures 1 and 2.

 $^{^{10}}$ The results reported by GMPT are different from those obtained in this study. GMPT providing very little detail on the private duopoly, it is difficult to understand the reason for these differences.

¹¹Firms may adopt different technologies in some variants of the RT model. This is the case when the number of firms exceeds two (Röller and Tombak, 1993), if firms cannot observe the technological choice of their competitor before deciding on the quantities to be produced (Boyer, Jacques and Moreaux, 2000), if choices are delegated to managers who are strategically assigned a different goal from profit maximization (Bárcena-Ruiz and Olaizola, 2008), if the additional cost of flexible technology is not the same for both firms (He, Ding and Hua, 2012) or if firms can enter into extensive collusion agreements on technological choices (Jacques, 2021).

The incentives of the public firm to invest in flexible technology are always higher than those of the private firm. This result is due to the fact that the state-owned firm takes into account the consumers surplus. Adoption of F technology increases competition between firms and benefits consumers.¹² The public firm also takes into account that if it adopts technology F, the private firm will reduce its production levels and will suffer a reduction in its profit. But the positive effect on the consumers surplus dominates the negative effect on the profit of the private firm. The state-owned firm therefore selects F technology more often than the private firm. There is an area where equilibrium is (D, F), but none where equilibrium is (F, D).¹³

It can also be emphasized that there is no zone of parameter values with multiple equilibria.

Comparison: A comparison of the equilibria obtained in the mixed duopoly and in the private duopoly gives clear results. The area where (F, F) is an equilibrium is wider in a private duopoly than in a mixed duopoly. The area where (D, D) is an equilibrium is also wider in the private duopoly than in the mixed duopoly. The area where firms choose different technologies in the mixed duopoly totally encompasses the area where firms opt for opposite technologies in the private duopoly.

Proposition 1 The shift from a private to a mixed duopoly increases the public firm's incentives to invest in flexible technology and reduces the private firm's incentives to choose flexible technology.

A public firm takes into account the beneficial effect of technology F on the surplus of consumers. This increases its incentives to invest in flexible technology. A private firm confronted with a public firm anticipates that its production levels will be lower than if it were opposed to another private firm, which reduces its incentives to invest in more expensive technology to increase its product range.

4 Sequential choices

In this section, we will investigate whether the order in which firms choose their technology has an impact on the technological equilibrium configuration. So we change the game's timeline, which now includes three stages. In the first, the leading firm chooses its technology. In the second, the other firm observes the technology adopted by the leading firm, then decides whether to acquire the F or D technology. In the third stage, the two firms compete in quantities. In this section, the leadership role is assigned to either firm exogenously. We'll make the timing endogenous in the next section.

 $^{^{12}}$ RT and Castanheira de Moura and Jacques (2002) have shown this in the case where the marginal cost of firms is constant in a private duopoly.

 $^{^{13}\}mathrm{Contrary}$ to the results presented by GMPT.

4.1 The public firm is the leader

We start with the case where the leadership role is assigned to the public firm. If the equilibrium of the simultaneous play is (D, D) or (F, F), the modification of the chronology of the play has no impact on the equilibrium configuration.

Nor does it have any in the area above the best response of the private firm to D and below the best response of the public firm to D. This area covers zones 2 and 3, as well as the top of zone 4. In this area, the private firm acquires a technology D regardless of the technological choice of the public firm. The public company therefore chooses a technology F. The equilibrium configuration is therefore (D, F) as in the simultaneous game.

The bottom of zone 4, more precisely the area between the two best response functions of the private firm to the technological choice of the public firm, is more interesting. In this area, the equilibrium of the simultaneous play is (D, F). But, in the sequential game, if the public firm modifies its technology and opts for D, the private firm will, in return, change its technology and select F. The public firm therefore has the choice between configurations (D, F) and (F, D). She prefers the second if and only if:

$$TS(F,D) \ge TS(D,F) \Leftrightarrow \frac{\left(1549 - 674\lambda - 548\lambda^2 + 250\lambda^3 - \lambda^4\right) \left(33 - 5\lambda^2\right)^2}{32\left(11 - 3\lambda^2\right)^2 \left(447 - 177\lambda - 63\lambda^2 + 25\lambda^3\right)} \ge 1$$

The ratio to the right of the inequality is always less than 1. The state-owned firm therefore always prefers (D, F) to (F, D). The equilibria obtained, in the mixed duopoly, when the public firm is leader are identical to the equilibrium of the game where the technological choices are simultaneous.

4.2 The private firm is the leader

It is now assumed that the private firm is the first to make its technological choice. This does not change the technological configuration if the equilibrium of the simultaneous play is (D, D) or (F, F). A change can only occur in the area where (D, F) is the equilibrium of the simultaneous play. Below the best response of the public firm to F, the private firm cannot influence the technological choice of the public firm. For the public firm acquiring a flexible strategy is a dominant strategy. The private firm can therefore do no better than to opt for D. We thus obtain the same equilibrium (D, F) as in the simultaneous game. On the other hand, in the area between the two best response functions of the public firm (the top of zone 2), the private firm can impose the configuration (F, D) by adopting the F technology before the public firm chooses its technology. In this zone, the private firm therefore has the choice between configurations (F, D) and (D, F). It selects the first if and only if:

$$\pi_{1}(F,D) \ge \pi_{1}(D,F) \Leftrightarrow \frac{370 - 292\lambda - 42\lambda^{2} + 72\lambda^{3} - 12\lambda^{4}}{16\left(11 - 3\lambda^{2}\right)^{2}} - \frac{8\left(3 - \lambda\right)^{2}}{\left(33 - 5\lambda^{2}\right)^{2}} \ge \frac{s}{a^{2}}$$

This border is located above the border where the best response of the public firm to a dedicated technology is a flexible technology. The private firm chooses F and the public firm reacts by selecting D.

In short, when the private firm is a leader, we obtain the following technological equilibria.



Figure 2: Technological equilibria when the private firm is the leader

When the private firm is the leader, there is an area where (F, D) is an equilibrium in a mixed duopoly. It is recalled that this configuration never appears, in the mixed duopoly, when the technological choices of the firms are simultaneous. Changing the game's chronology can therefore reverse the technological choices of firms when the private firm becomes a leader. This reversal leads to a reduction in the consumer surplus and the social welfare.¹⁴

In this area, the technological equilibrium configuration in a private duopoly is (D, D). It is therefore possible that the mutation from a private duopoly to a mixed duopoly will lead to a transition to the flexible technology of the firm that remains private, but this can only happen if this firm makes its technological choice before the public firm.

Proposition 2 A private firm may choose a more flexible technology if it is confronted with a public firm than if it is opposed to a private firm if (and only if) it chooses its technology before its competitor.

¹⁴We saw above that we always have: $\overline{TS(F,D)} \ge TS(D,F)$.

5 Endogenous timing

In the previous sections, the timing of the technological choices was exogenous. In this section, we will make it endogenous by considering the game with observable delay proposed by Hamilton and Slutsky (1990).

In this variant, the game breaks down into four stages. In the first stage, each firm simultaneously announces whether it will choose the technology in the second or third stage. This announcement is engaging. In steps 2 and 3, firms choose their technology according to the timing on which they are committed. In the fourth stage, firms compete in quantities.

We have seen above that the technological configuration is independent of the order of the choices of the firms, with the exception of the zone where the equilibrium is (F, D) if the private firm is the leader and (D, F) in the other possible timings. In this area, the private firm prefers to be leader to play at the same time as the public firm. Moreover, she is indifferent between playing at the same time as the public firm and being a follower. For the private firm, announcing that it will choose its technology in stage 2 is a weakly dominant strategy. Similarly, making its technological choice in stage 2 is a weakly dominant strategy for the state-owned firm. The latter prefers to play at the same time as the private firm rather than to be a follower and it is indifferent between being a leader and playing at the same time as the private firm.

If we eliminate the weakly dominated strategies, we get the following result:

Proposition 3 In a mixed duopoly, the two firms want to adopt their technology as soon as possible. Simultaneous timing is the one that emerges at equilibrium when the timing is endogenous.

If we keep the weakly dominated strategies, the timing where the public firm is the leader and the private firm plays second is also a perfect Nash equilibrium of the game.

The technological configuration (F, D) is never an equilibrium in the game with endogenous timing.

6 Impact of privatisation on the welfare

In this section, we compare the social surpluses obtained in a mixed duopoly and in a private duopoly in order to determine whether the privatization of the public firm can increase the social surplus. We first analyse the case where technological choices are simultaneous, then the case where they are sequential.

6.1 Simultaneous choices

In zones 1, 3 and 5 (in Figure 1), privatization of the public firm does not change the technological choices of firms. However, it changes the quantities produced by each of the firms. In these areas, privatization leads

to a reduction in the social surplus.¹⁵

In zone 2, the privatization of the public firm leads to a change in the technological equilibrium configuration, from (D, F) to (D, D). Comparing the social surpluses in both situations,¹⁶ we observe that privatization decreases the social surplus.

In zone 4, the privatization of the state-owned firm is also followed by a change in the technological configuration. The direction of this change, however, is opposed to that of zone 2. In zone 4, privatization results in increased flexibility for industry. The equilibrium technology configuration changes from (D, F) to (F, F). The private firm expands its product range and increases its production if the public firm is privatized. Privatization increases the social surplus if and only if:

$$\frac{4(3+2\lambda)}{(5+3\lambda)^2}a^2 - 2F_F \geq \frac{447 - 177\lambda - 63\lambda^2 + 25\lambda^3}{(33-5\lambda^2)^2}a^2 - F_D - F_F$$

$$\Leftrightarrow \frac{4(3+2\lambda)}{(5+3\lambda)^2} - \frac{447 - 177\lambda - 63\lambda^2 + 25\lambda^3}{(33-5\lambda^2)^2} \geq \frac{s}{a^2}$$

This condition is checked for certain parameter values. The area where this occurs (zone 4a) can be viewed by representing the previous condition in Figure 1.





In summary, privatization of the public firm can only increase the social surplus if (1) the initial technolog-

¹⁵See Appendix for details of the calculations of social surplus comparisons.

 $^{^{16}\}mathrm{See}$ Appendix.

ical configuration is (D, F), (2) privatization induces the competing firm to adopt a more flexible technology and (3) the differentiation between the two goods is relatively strong.

Proposition 4 Privatization of the public firm may increase the social surplus if it induces the private firm to adopt a more flexible technology.

6.2 Sequential choices

If the equilibrium technological configuration when the choices are sequential is identical to that obtained when the choices are simultaneous, the previous results will continue to apply. In particular, in the area where privatization is optimal when technological choices are simultaneous, privatization remains socially desirable when technological choices are sequential.

It remains to analyse the consequences of privatization in the area where the equilibrium is (F, D) in the mixed duopoly when the private firm is the leader. This is, in fact, the only area where a sequential equilibrium is different from the equilibrium of the simultaneous game. In this area, when the private firm is the leader, privatisation leads to a change from (F, D) to (D, D). Privatization leads to a reduction in the private firm's product range. This contraction has a negative effect on the consumer surplus. However, it is accompanied by a reduction in the firm's fixed costs, which are relatively high in this area. This second effect can be beneficial for the social surplus. In this area, privatization increases the social surplus if and only if:

$$\frac{5+\lambda}{(4+\lambda)^2}a^2 - 2F_D \ge \frac{1549 - 674\lambda - 548\lambda^2 + 250\lambda^3 - \lambda^4}{32(11 - 3\lambda^2)^2}a^2 - F_F - F_D$$
$$\Leftrightarrow \frac{s}{a^2} \ge \frac{1549 - 674\lambda - 548\lambda^2 + 250\lambda^3 - \lambda^4}{32(11 - 3\lambda^2)^2} - \frac{5+\lambda}{(4+\lambda)^2}$$

This boundary passes below the frontier delineating the area where (F, D) is the equilibrium. The condition is therefore checked throughout the area where (F, D) is chosen in the mixed duopoly when the private firm is the leader. In this area, it is optimal to privatize the state-owned firm.

Proposition 5 When the private firm is the leader, the privatization of the public firm is desirable throughout the area where the technological configuration is (F, D).

7 Conclusion

In this study, we looked at the impact of firm ownership, as well as the timing of choices on decisions to adopt a flexible or dedicated technology in a duopoly.

In a mixed duopoly, the two firms equip themselves with flexible technology when the additional cost of this technology (s) is small relative to the size of the potential demand (measured by a^2). In contrast, if

the ratio s/a^2 is high, both firms acquire dedicated technologies. For the intermediate values of s/a^2 , the technological equilibrium configuration is asymmetrical. The public company chooses flexible technology and the private company chooses dedicated technology. The reverse technological configuration never appears in equilibrium. In a private duopoly, we find the same classification of the different possible technological configurations according to s/a^2 . However, the boundaries of the different zones are different. In particular, the area where the configuration is asymmetric in the private duopoly is totally included in the area where the technological choices of the two firms are different in the mixed duopoly. It therefore appears that the public ownership of one of the firms increases its incentives to equip itself with flexible technology and reduces that of its private competitor to acquire flexible technology.

When the private firm can choose its technology before the public firm, a new technological configuration emerges in equilibrium for certain parameter values. There is a zone of parameter values in which the private firm operates a flexible production line while the public firm limits its investments to the acquisition of a line dedicated to the production of a single product. The range of products offered by the private firm is then wider than that of the state-owned firm. In this area, we observe a reversal of the technologies of firms in relation to the game where the technological choices are simultaneous. This reversal allows the private firm to increase its profits, but it results in a decrease in the consumer surplus and the social surplus.

When the order of technological choices has an impact on the equilibrium technological configuration, the private firm prefers the situation in which it is the leader while the public firm prefers the other timings. Each of the firms wishes to commit to the earliest date to decide on its technological choice. The endogenous timing of equilibrium is one where technological choices are simultaneous.

The privatization of the state-owned firm never increases the social surplus, if this privatization does not change the technological choice of the private firm. On the other hand, privatization may be desirable for certain parameter values if it induces the private firm to change technology.

This study could, in future research, be extended in several directions. It would also be interesting to study alternative timings during the competition phase in quantities. We could also analyze the impact of a partial privatization of the public firm or of foreign investors holding a share of the private firm's capital.

8 Appendix

8.1 Cournot competition

8.1.1 Private duopoly

Both firms have dedicated technology: We calculate the best response from each firm:

$$\pi_1 \left(q_1^A, q_2^B \right) = p^A \left(q_1^A, q_2^B \right) q_1^A - \left(q_1^A \right)^2 - F_D = \left(a - q_1^A - \lambda q_2^B \right) q_1^A - \left(q_1^A \right)^2 - F_D$$
$$\frac{\partial \pi_1}{\partial q_1^A} \left(q_1^A, q_2^B \right) = 0 \Leftrightarrow q_1^A = \frac{1}{4} \left(a - \lambda q_2^B \right)$$

Equilibrium quantities:

$$\left\{\begin{array}{l}q_1^A = \frac{1}{4}\left(a - \lambda q_2^B\right)\\q_2^B = \frac{1}{4}\left(a - \lambda q_1^A\right)\end{array}\right\} \Leftrightarrow \left\{\begin{array}{l}q_1^A = \frac{1}{4+\lambda}a\\q_2^B = \frac{1}{4+\lambda}a\end{array}\right\}$$

Both firms have flexible technology:

$$\pi_{1} \left(q_{1}^{A}, q_{2}^{A}, q_{1}^{B}, q_{2}^{B}\right) = p^{A} \left(q_{1}^{A}, q_{2}^{A}, q_{1}^{B}, q_{2}^{B}\right) q_{1}^{A} - \left(q_{1}^{A}\right)^{2} + p^{B} \left(q_{1}^{A}, q_{2}^{A}, q_{1}^{B}, q_{2}^{B}\right) q_{1}^{B} - \left(q_{1}^{B}\right)^{2} - F_{F}$$

$$\frac{\partial \pi_{1}}{\partial q_{1}^{A}} \left(q_{1}^{A}, q_{2}^{A}, q_{1}^{B}, q_{2}^{B}\right) = 0 \Leftrightarrow a - 4q_{1}^{A} - q_{2}^{A} - 2\lambda q_{1}^{B} - \lambda q_{2}^{B} = 0$$

$$\frac{\partial \pi_{1}}{\partial q_{1}^{B}} \left(q_{1}^{A}, q_{2}^{A}, q_{1}^{B}, q_{2}^{B}\right) = 0 \Leftrightarrow a - 4q_{1}^{B} - q_{2}^{B} - 2\lambda q_{1}^{A} - \lambda q_{2}^{A} = 0$$

Cournot equilibrium:

$$\left\{ \begin{array}{l} a - 4q_1^A - q_2^A - 2\lambda q_1^B - \lambda q_2^B = 0\\ a - 4q_1^B - q_2^B - 2\lambda q_1^A - \lambda q_2^A = 0\\ a - q_1^A - 4q_2^A - \lambda q_1^B - 2\lambda q_2^B = 0\\ a - q_1^B - 4q_2^B - \lambda q_1^A - 2\lambda q_2^B = 0 \end{array} \right\} \Leftrightarrow q_1^A = q_2^A = q_1^B = q_2^B = \frac{1}{5 + 3\lambda} a$$

Firms have different technologies: We will assume that firm 1 has a dedicated technology. We characterize its best response to firm 2 productions:

$$\pi_1 \left(q_1^A, q_2^A, q_2^B \right) = p^A \left(q_1^A, q_2^A, q_2^B \right) q_1^A - \left(q_1^A \right)^2 - F_D = \left(a - q_1^A - q_2^A - \lambda q_2^B \right) q_1^A - \left(q_1^A \right)^2 - F_D$$

$$\frac{\partial \pi_1}{\partial q_1^A} \left(q_1^A, q_2^A, q_2^B \right) = 0 \Leftrightarrow a - 4q_1^A - q_2^A - \lambda q_2^B = 0$$

We determine the best replies from firm 2 (which has flexible technology):

$$\pi_{2} \left(q_{1}^{A}, q_{2}^{A}, q_{2}^{B}\right) = p^{A} \left(q_{1}^{A}, q_{2}^{A}, q_{2}^{B}\right) q_{2}^{A} - \left(q_{2}^{A}\right)^{2} + p^{B} \left(q_{1}^{A}, q_{2}^{A}, q_{2}^{B}\right) q_{2}^{B} - \left(q_{2}^{B}\right)^{2} - F_{F}$$

$$\frac{\partial \pi_{2}}{\partial q_{2}^{A}} \left(q_{1}^{A}, q_{2}^{A}, q_{2}^{B}\right) = 0 \Leftrightarrow a - 4q_{2}^{A} - q_{1}^{A} - 2\lambda q_{2}^{B} = 0$$

$$\frac{\partial \pi_{2}}{\partial q_{2}^{B}} \left(q_{1}^{A}, q_{2}^{A}, q_{2}^{B}\right) = 0 \Leftrightarrow a - 4q_{2}^{B} - \lambda q_{1}^{A} - 2\lambda q_{2}^{A} = 0$$

Cournot equilibrium:

$$\left\{ \begin{array}{c} a - 4q_1^A - q_2^A - \lambda q_2^B = 0\\ a - 4q_2^A - q_1^A - 2\lambda q_2^B = 0\\ a - 4q_2^B - \lambda q_1^A - 2\lambda q_2^A = 0 \end{array} \right\} \Leftrightarrow \left\{ \begin{array}{c} q_2^A = \frac{12 - 7\lambda + \lambda^2}{4(15 - 4\lambda^2)}a\\ q_1^A = \frac{6 - \lambda^2}{2(15 - 4\lambda^2)}a\\ q_2^B = \frac{3(5 - 3\lambda)}{4(15 - 4\lambda^2)}a \end{array} \right\}$$

8.1.2 Mixed duopoly

Both firms have dedicated technology: This case is similar to the case without merger in Bárcena-Ruiz and Garzón (2003).

The private firm seeks to maximize its profit. Its best reply to the quantity produced by the public firm is therefore given by:

$$\pi_1 \left(q_1^A, q_2^B \right) = p^A \left(q_1^A, q_2^B \right) q_1^A - \left(q_1^A \right)^2 - F_D = \left(a - q_1^A - \lambda q_2^B \right) q_1^A - \left(q_1^A \right)^2 - F_D$$
$$\frac{\partial \pi_1}{\partial q_1^A} \left(q_1^A, q_2^B \right) = 0 \Leftrightarrow q_1^A = \frac{1}{4} \left(a - \lambda q_2^B \right)$$

The public firm seeks to maximize the social surplus. Its best response to the quantity produced by the private firm is obtained as follows:

$$TS(q_{1}^{A}, q_{2}^{B}) = p^{A}(q_{1}^{A}, q_{2}^{B})q_{1}^{A} - (q_{1}^{A})^{2} - F_{D} + p^{B}(q_{1}^{A}, q_{2}^{B})q_{2}^{B} - (q_{2}^{B})^{2} - F_{D} + \frac{1}{2}\left[\left(q_{1}^{A}\right)^{2} + \left(q_{2}^{B}\right)^{2}\right] + \lambda q_{1}^{A}q_{2}^{B}$$
$$\frac{\partial TS}{\partial q_{2}^{B}}(q_{1}^{A}, q_{2}^{B}) = 0 \Leftrightarrow q_{2}^{B} = \frac{1}{3}\left(a - \lambda q_{1}^{A}\right)$$
Cournot equilibrium:

$$\left\{\begin{array}{l}q_1^A = \frac{1}{4}\left(a - \lambda q_2^B\right)\\q_2^B = \frac{1}{3}\left(a - \lambda q_1^A\right)\end{array}\right\} \Leftrightarrow \left\{\begin{array}{l}q_1^A = \frac{3 - \lambda}{12 - \lambda^2}a\\q_2^B = \frac{4 - \lambda}{12 - \lambda^2}a\end{array}\right\}$$

It should be noted that $q_2^B > q_1^A$. This is a classic result in mixed duopolies. The state-owned firm takes into account the impact of an increase in its production on consumers. It therefore produces more than a private firm would in a private duopoly.¹⁷ As quantities are strategic substitutes, the private firm reacts to this increase in production by reducing its own production.

Both firms have flexible technology: We start by determining the best replies from the private firm:

$$\pi_{1}\left(q_{1}^{A}, q_{2}^{A}, q_{1}^{B}, q_{2}^{B}\right) = p^{A}\left(q_{1}^{A}, q_{2}^{A}, q_{1}^{B}, q_{2}^{B}\right)q_{1}^{A} - \left(q_{1}^{A}\right)^{2} + p^{B}\left(q_{1}^{A}, q_{2}^{A}, q_{1}^{B}, q_{2}^{B}\right)q_{1}^{B} - \left(q_{1}^{B}\right)^{2} - F_{F}$$

$$= \left(a - q_{1}^{A} - q_{2}^{A} - \lambda q_{1}^{B} - \lambda q_{2}^{B}\right)q_{1}^{A} - \left(q_{1}^{A}\right)^{2} + \left(a - q_{1}^{B} - q_{2}^{B} - \lambda q_{1}^{A} - \lambda q_{2}^{A}\right)q_{1}^{B} - \left(q_{1}^{B}\right)^{2} - F_{F}$$

¹⁷The marginal cost of the public firm is equal to the equilibrium price of the good B:

$$Cm_2\left(q_2^B\right) = 2q_2^B = 2\frac{4-\lambda}{12-\lambda^2}a = p^B = \frac{8-2\lambda}{12-\lambda^2}a$$

$$\frac{\partial \pi_1}{\partial q_1^A} \left(q_1^A, q_2^A, q_1^B, q_2^B \right) = 0 \Leftrightarrow a - 4q_1^A - q_2^A - 2\lambda q_1^B - \lambda q_2^B = 0 \\ \frac{\partial \pi_1}{\partial q_1^B} \left(q_1^A, q_2^A, q_1^B, q_2^B \right) = 0 \Leftrightarrow a - 4q_1^B - q_2^B - 2\lambda q_1^A - \lambda q_2^A = 0$$

We then characterize the best replies of the public firm:

$$TS(q_{1}^{A}, q_{2}^{A}, q_{1}^{B}, q_{2}^{B}) = p^{A}(.)q_{1}^{A} - (q_{1}^{A})^{2} + p^{B}(.)q_{1}^{B} - (q_{1}^{B})^{2} + p^{A}(.)q_{2}^{A} - (q_{2}^{A})^{2} + p^{B}(.)q_{2}^{B} - (q_{2}^{B})^{2} -2F_{F} + \frac{1}{2}\left[(q_{1}^{A} + q_{2}^{A})^{2} + (q_{1}^{B} + q_{2}^{B})^{2}\right] + \lambda(q_{1}^{A} + q_{2}^{A})(q_{1}^{B} + q_{2}^{B})$$

$$\frac{\partial TS}{\partial q_2^A} \begin{pmatrix} q_1^A, q_2^A, q_1^B, q_2^B \end{pmatrix} = 0 \Leftrightarrow a - q_1^A - 3q_2^A - \lambda q_1^B - \lambda q_2^B = 0$$
$$\frac{\partial TS}{\partial q_2^B} \begin{pmatrix} q_1^A, q_2^A, q_1^B, q_2^B \end{pmatrix} = 0 \Leftrightarrow a - q_1^B - 3q_2^B - \lambda q_1^A - \lambda q_2^A = 0$$

Cournot equilibrium:

$$\left\{ \begin{array}{l} a - 4q_1^A - q_2^A - 2\lambda q_1^B - \lambda q_2^B = 0\\ a - 4q_1^B - q_2^B - 2\lambda q_1^A - \lambda q_2^A = 0\\ a - q_1^A - 3q_2^A - \lambda q_1^B - \lambda q_2^B = 0\\ a - q_1^B - 3q_2^B - \lambda q_1^A - \lambda q_2^A = 0 \end{array} \right\} \Leftrightarrow \left\{ \begin{array}{l} q_2^A = q_2^B = \frac{3+\lambda}{11+8\lambda+\lambda^2}a\\ q_1^A = q_1^B = \frac{2}{11+8\lambda+\lambda^2}a \end{array} \right\}$$

As in the previous case, it can be noted that the output of the public firm is higher than that of the private firm.

The private firm has a dedicated technology and the public firm is flexible: Best response from the private firm:

$$\pi_1 \left(q_1^A, q_2^A, q_2^B \right) = p^A \left(q_1^A, q_2^A, q_2^B \right) q_1^A - \left(q_1^A \right)^2 - F_D$$
$$\frac{\partial \pi_1}{\partial q_1^A} \left(q_1^A, q_2^A, q_2^B \right) = 0 \Leftrightarrow a - 4q_1^A - q_2^A - \lambda q_2^B = 0$$

Best response from the state-owned firm:

$$TS(q_{1}^{A}, q_{2}^{A}, q_{2}^{B}) = p^{A}(.) q_{1}^{A} - (q_{1}^{A})^{2} - F_{D} + p^{A}(.) q_{2}^{A} - (q_{2}^{A})^{2} + p^{B}(.) q_{2}^{B} - (q_{2}^{B})^{2} - F_{F} + \frac{1}{2} \left[(q_{1}^{A} + q_{2}^{A})^{2} + (q_{2}^{B})^{2} \right] + \lambda (q_{1}^{A} + q_{2}^{A}) q_{2}^{B}$$

$$\frac{\partial TS}{\partial q_2^A} \left(q_1^A, q_2^A, q_2^B \right) = 0 \Leftrightarrow a - q_1^A - 3q_2^A - \lambda q_2^B = 0$$
$$\frac{\partial TS}{\partial q_2^B} \left(q_1^A, q_2^A, q_2^B \right) = 0 \Leftrightarrow a - 3q_2^B - \lambda q_1^A - \lambda q_2^A = 0$$

Cournot equilibrium:

$$\left\{\begin{array}{c}a - 4q_1^A - q_2^A - \lambda q_2^B = 0\\a - q_1^A - 3q_2^A - \lambda q_2^B = 0\\a - 3q_2^B - \lambda q_1^A - \lambda q_2^A = 0\end{array}\right\} \Leftrightarrow \left\{\begin{array}{c}q_1^A = \frac{2(3-\lambda)}{33-5\lambda^2}a\\q_2^A = \frac{3(3-\lambda)}{33-5\lambda^2}a\\q_2^B = \frac{11-5\lambda}{33-5\lambda^2}a\end{array}\right\}$$

The private firm is flexible and the public firm has a dedicated technology: Best replies from the private firm:

$$\pi_{1} \left(q_{1}^{A}, q_{1}^{B}, q_{2}^{B} \right) = p^{A} \left(q_{1}^{A}, q_{1}^{B}, q_{2}^{B} \right) q_{1}^{A} - \left(q_{1}^{A} \right)^{2} + p^{B} \left(q_{1}^{A}, q_{1}^{B}, q_{2}^{B} \right) q_{1}^{B} - \left(q_{1}^{B} \right)^{2} - F_{F}$$

$$= \left(a - q_{1}^{A} - \lambda q_{1}^{B} - \lambda q_{2}^{B} \right) q_{1}^{A} - \left(q_{1}^{A} \right)^{2} + \left(a - q_{1}^{B} - q_{2}^{B} - \lambda q_{1}^{A} \right) q_{1}^{B} - \left(q_{1}^{B} \right)^{2} - F_{F}$$

$$\frac{\partial \pi_{1}}{\partial q_{1}^{A}} \left(q_{1}^{A}, q_{1}^{B}, q_{2}^{B} \right) = 0 \Leftrightarrow a - 4q_{1}^{A} - 2\lambda q_{1}^{B} - \lambda q_{2}^{B} = 0$$

$$\frac{\partial \pi_{1}}{\partial q_{1}^{B}} \left(q_{1}^{A}, q_{1}^{B}, q_{2}^{B} \right) = 0 \Leftrightarrow a - 4q_{1}^{B} - q_{2}^{B} - 2\lambda q_{1}^{A} = 0$$

Best reply from the public firm:

$$TS\left(q_{1}^{A}, q_{1}^{B}, q_{2}^{B}\right) = p^{A}\left(.\right)q_{1}^{A} - \left(q_{1}^{A}\right)^{2} + p^{B}\left(.\right)q_{1}^{B} - \left(q_{1}^{B}\right)^{2} - F_{F} + p^{B}\left(.\right)q_{2}^{B} - \left(q_{2}^{B}\right)^{2} - F_{D} + \frac{1}{2}\left[\left(q_{1}^{A}\right)^{2} + \left(q_{1}^{B} + q_{2}^{B}\right)^{2}\right] + \lambda q_{1}^{A}\left(q_{1}^{B} + q_{2}^{B}\right) \\ \frac{\partial TS}{\partial q_{2}^{B}}\left(q_{1}^{A}, q_{1}^{B}, q_{2}^{B}\right) = 0 \Leftrightarrow a - q_{1}^{B} - 3q_{2}^{B} - \lambda q_{1}^{A} = 0$$

Cournot equilibrium:

$$\left\{\begin{array}{c}a - 4q_1^A - 2\lambda q_1^B - \lambda q_2^B = 0\\a - 4q_1^B - q_2^B - 2\lambda q_1^A = 0\\a - q_1^B - 3q_2^B - \lambda q_1^A = 0\end{array}\right\} \Leftrightarrow \left\{\begin{array}{c}q_1^A = \frac{11 - 7\lambda}{4(11 - 3\lambda^2)}a\\q_2^B = \frac{12 - 2\lambda - 2\lambda^2}{4(11 - 3\lambda^2)}a\\q_1^B = \frac{8 - 5\lambda + \lambda^2}{4(11 - 3\lambda^2)}a\end{array}\right\}$$

8.2 Impact of privatisation on the welfare

8.2.1 In zone 5

Privatization has no impact on the equilibrium technological configuration, which is (F, F) in both types of duopoly. By comparing the social surpluses, we obtain that privatization increases the social surplus if and only if:

$$\frac{4(3+2\lambda)}{(5+3\lambda)^2}a^2 - 2F_F \ge \frac{59+55\lambda+13\lambda^2+\lambda^3}{\left(11+8\lambda+\lambda^2\right)^2}a^2 - 2F_F \Leftrightarrow \frac{4(3+2\lambda)\left(11+8\lambda+\lambda^2\right)^2}{\left(59+55\lambda+13\lambda^2+\lambda^3\right)\left(5+3\lambda\right)^2} \ge 1$$

The left-hand ratio of the inequality is always less than 1. So this condition is never fulfilled. In this area, privatization leads to a reduction in the social surplus.

8.2.2 In zone 3

Privatization does not change the technological equilibrium,¹⁸ which remains (D, F). Privatization causes an increase in the social surplus if and only if:

$$\frac{2853 - 1206\lambda - 1000\lambda^2 + 438\lambda^3 + 3\lambda^4}{32\left(15 - 4\lambda^2\right)^2}a^2 - F_D - F_F \ge \frac{447 - 177\lambda - 63\lambda^2 + 25\lambda^3}{\left(33 - 5\lambda^2\right)^2}a^2 - F_D - F_F$$

¹⁸After privatization, the two firms can reverse their technological choice and move to equilibrium (F, D), but this has no impact on the social surplus.

$$\Leftrightarrow \frac{\left(2853 - 1206\lambda - 1000\lambda^{2} + 438\lambda^{3} + 3\lambda^{4}\right)\left(33 - 5\lambda^{2}\right)^{2}}{32\left(15 - 4\lambda^{2}\right)^{2}\left(447 - 177\lambda - 63\lambda^{2} + 25\lambda^{3}\right)} \ge 1$$

This condition is never verified. Privatization therefore reduces the social surplus in zone 3.

8.2.3 In zone 2

In zone 2, the privatisation of the public firm led to a change in the equilibrium technological configuration from (D, F) to (D, D). Privatization increases the social surplus if and only if:

$$\frac{5+\lambda}{(4+\lambda)^2}a^2 - 2F_D \geq \frac{447 - 177\lambda - 63\lambda^2 + 25\lambda^3}{(33 - 5\lambda^2)^2}a^2 - F_D - F_F$$

$$\Leftrightarrow \frac{s}{a^2} \geq \frac{447 - 177\lambda - 63\lambda^2 + 25\lambda^3}{(33 - 5\lambda^2)^2} - \frac{5+\lambda}{(4+\lambda)^2}$$

This inequality is never verified. The privatization of the public firm leads to a reduction in the social surplus.

8.2.4 In zone 1

Privatization has no impact on the technological equilibrium configuration, which is (D,D) in both cases. By comparing the social surpluses, we obtain that privatization increases the social surplus if and only if:

$$\frac{5+\lambda}{\left(4+\lambda\right)^2}a^2 - 2F_D \ge \frac{93 - 30\lambda - 6\lambda^2 + 2\lambda^3}{2\left(12 - \lambda^2\right)^2}a^2 - 2F_D \Leftrightarrow \frac{2\left(5+\lambda\right)\left(12 - \lambda^2\right)^2}{\left(4+\lambda\right)^2\left(93 - 30\lambda - 6\lambda^2 + 2\lambda^3\right)} \ge 1$$

This inequality is never verified. The privatization of the public firm leads to a reduction in the social surplus.

References

- ANAM Mahmudul, Syed A. BASHER and Shin-Hwan CHIANG (2007), Mixed oligopoly under demand uncertainty, *The B.E. Journal of Theoretical Economics*, Topics, 7 (1), Article 24.
- [2] BÁRCENA-RUIZ Juan Carlos (2007), Endogenous timing in a mixed duopoly: price competition, Journal of Economics, 91 (3), 263-272.
- [3] BÁRCENA-RUIZ Juan Carlos and F. Javier CASADO-IZAGA (2012), Location of public and private firms under endogenous timing of choices, *Journal of Economics*, 105 (2), 129-143.
- [4] BÁRCENA-RUIZ Juan Carlos and María Begoña GARZÓN (2003), Mixed duopoly, merger and multiproduct firms, *Journal of Economics*, 80 (1), 27-42.
- [5] BÁRCENA-RUIZ Juan Carlos and Norma OLAIZOLA (2008), Choice of flexible production technologies under strategic delegation, Japan and the World Economy, 20, 395-414.
- [6] BOYER Marcel, Armel JACQUES and Michel MOREAUX (2000), Observability and product flexibility in oligopoly, mimeo, CIRANO.
- [7] BOYER Marcel, Armel JACQUES and Michel MOREAUX (2002), Observation, flexibilité et structures technologiques des industries, Annales d'Économie et de Statistique, 65, 173-194.
- [8] BOYER Marcel and Michel MOREAUX (1997), Capacity commitment versus flexibility, Journal of Economics and Management Strategy, 6, 347-376.
- [9] CASTANHEIRA DE MOURA Micael and Armel JACQUES (2002), Consumers prefer flexible firms: A note on 'Strategic choice of flexible production technologies and welfare implications', mimeo.
- [10] GIL-MOLTÓ Maria José and Joanna POYAGO-THEOTOKY (2008), Flexible versus dedicated technology adoption in the presence of a public firm, Southern Economic Journal, 74 (4), 997-1016.
- [11] HAMILTON Jonathan H. and Steven M. SLUTSKY (1990), Endogenous timing in duopoly games: Stackelberg or Cournot equilibria, *Games and Economic Behavior*, 2, 29-46.
- [12] HE Ping, Husong DING and Zhongsheng HUA (2012), Strategic choice of flexible production technology using game theory approach, *Robotics and Computer-Integrated Manufacturing*, 28, 416-424.
- [13] JACQUES Armel (2003), La flexibilité technologique: un survol de la littérature, Revue d'économie politique, 113, 587-624.
- [14] JACQUES Armel (2004), Endogenous timing in a mixed oligopoly: a forgotten equilibrium, *Economics Letters*, 83 (2), 147-148.

- [15] JACQUES Armel (2006), Technologies flexibles et collusion tacite, Recherches Économiques de Louvain, 72 (4), 385-412.
- [16] JACQUES Armel (2021), Endogenous breadth of collusive agreements: an application to flexible technological choices, WP TEPP.
- [17] KIM Taekwon, Lars-Hendrik RÖLLER and Mihkel TOMBAK (1992), Strategic choice of flexible production technologies and welfare implications: addendum et corrigendum, *Journal of Industrial Economics*, 40, 233-235.
- [18] LU Yuanzhu (2006), Endogenous timing in a mixed oligopoly with foreign competitors: the linear demand case, *Journal of Economics*, 88 (1), 49-68.
- [19] MATSUMURA Toshihiro (2003a), Stakelberg mixed duopoly with a foreign competitor, Bulletin of Economic Research, 55 (3), 275-287.
- [20] MATSUMURA Toshihiro (2003b), Endogenous role in mixed markets: a two production period model, Southern Economic Journal, 70 (2), 403-413.
- [21] MATSUMURA Toshihiro and Akira OGAWA (2010), On the robutness of private leadership in mixed duopoly, Australian Economic Papers, 49, 149-160.
- [22] MÉNDEZ-NAYA José (2015), Endogenous timing in a mixed duopoly model, Journal of Economics, 116, 165-174.
- [23] PAL Debashis (1998), Endogenous timing in a mixed oligopoly, *Economics Letters*, 61, 181-185.
- [24] RÖLLER Lars-Hendrik and Mihkel TOMBAK (1990), Strategic choice of flexible production technologies and welfare implications, *Journal of Industrial Economics*, 38, 417-431.
- [25] RÖLLER Lars-Hendrik and Mihkel TOMBAK (1993), Competition and investment in flexible technologies, *Management Science*, 39, 107-114.
- [26] ZHANG Jianhu and Changying LI (2013), Endogenous timing in a mixed oligopoly under demand uncertainty, *Journal of Economics*, 108 (3), 273-289.
- [27] ZIKOS Vasileios (2007a), Equilibrium and optimal R&D roles in a mixed market, mimeo.

22-3. Reducing ethnic discrimination through formal warning : evidence from two combined field experiments

Sylvain Chareyron, Yannick L'Horty, Souleymane Mbaye, Pascale Petit

22-2. Cream skimming and Discrimination in access to medical care: a field experiment Sylvain Chareyron, Yannick L'horty, Pascale Petit

22-1. Optimal taxation with multiple incomes and types

Kevin Spiritus, Etienne Lehmann, Sander Renes, Floris T. Zoutman

21-11. Intermittent collusive agreements : antitrust policy and business cycles Emilie Dargaud, Armel Jacques

21-10. Endogenous breadth of collusive agreements : an application to flexible technological choices

Emilie Dargaud, Armel Jacques

21-9. How to tax different incomes? Laurence Jacquet, Etienne Lehmann

21-8. Does optimal capital taxation under stochastic returns to savings Eddy Zanoutene

21-7. Does the gender mix influence collective bargaining on gender equality? Evidence from France

Anne-Sophie Bruno, Nathalie Greenan, Jérémy Tanguy

21-6. The effects of the non-financial component of business accelerators Fabrice Gilles, Yannick L'Horty, Ferhat Mihoubi

21-5. Organisational changes and long term sickness absence and injury leave Mohamed Ali Ben Halima, Nathalie Greenan, Joseph Lanfranchi

21-4. The unexplored discriminations towards youth : equal access to goods and services David Gray, Yannick L'Horty, Souleymane Mbaye, Pascale Petit

21-3. The zero effect of income tax on the timing of birth: some evidence on French data Nicolas Moreau

21-2. Tropical cyclones and fertility : new evidence from Madagascar Idriss Fontaine, Sabine Garabedian, David Nortes-Martinez, Hélène Vérèmes

21-1. On the heterogeneous impacts of the COVID-19 lockdown on US unemployment Malak Kandoussi, François Langot

20-8. COVID-19 mortality and health expenditures across European countries: The positive correlation puzzle

Serge Blondel, Radu Vranceanu

20-7. Measuring discrimination in the labour market Emmanuel Duguet

20-6. The effects of age on educational performances at the end of primary school: crosssectional and regression discontinuity approach applications from Reunion Island Daniel Rakotomalala

20-5. Slowdown antitrust investigations by decentralization Emilie Dargaud, Armel Jacques

20-4. Is international tourism responsible for the pandemic of COVID19? A preliminary cross-country analysis with a special focus on small islands Jean-François Hoarau

20-3. Does labor income react more to income tax or means tested benefit reforms? Michaël Sicsic

20-2. Optimal sickness benefits in a principal-agent model Sébastien Ménard

20-1. The specific role of agriculture for economic vulnerability of small island spaces Stéphane Blancard, Maximin Bonnet, Jean-François Hoarau

19-8. The impact of benefit sanctions on equilibrium wage dispersion and job vacancies Sebastien Menard

19-7. Employment fluctuations, job polarization and non-standard work: Evidence from France and the US

Olivier Charlot, Idriss Fontaine, Thepthida Sopraseuth

19-6. Counterproductive hiring discrimination against women: Evidence from French correspondence test

Emmanuel Duguet, Loïc du Parquet, Yannick L'Horty, Pascale Petit

19-5. Inefficient couples: Non-minimization of the tax burden among French cohabiting couples

Olivier Bargain, Damien Echevin, Nicolas Moreau, Adrien Pacifico

19-4. Seeking for tipping point in the housing market: evidence from a field experiment Sylvain Chareyron, Samuel Gorohouna, Yannick L'Horty, Pascale Petit, Catherine Ris

19-3. Testing for redlining in the labor market Yannick L'Horty, Mathieu Bunel, Pascale Petit

19-2. Labour market flows: Accounting for the public sector Idriss Fontaine, Ismael Galvez-Iniesta, Pedro Gomes, Diego Vila-Martin

19-1. The interaction between labour force participation of older men and their wife: **lessons from France** Idriss Fontaine

18-15. Be healthy, be employed: a comparison between the US and France based on a general equilibrium model

Xavier Fairise, François Langot, Ze Zhong Shang

18-14. Immigrants' wage performance in the routine biased technological change era: France 1994-2012

Catherine Laffineur, Eva Moreno-Galbis, Jeremy Tanguy, Ahmed Tritah

18-13. Welfare cost of fluctuations when labor market search interacts with financial frictions

Elini Iliopulos, François Langot, Thepthida Sopraseuth

18-12. Accounting for labor gaps François Langot, Alessandra Pizzo

18-11. Unemployment fluctuations over the life cycle Jean-Olivier Hairault, François Langot, Thepthida Sopraseuth

18-10. Layoffs, Recalls and Experience Rating Julien Albertini, Xavier Fairise

18-9. Environmental policy and health in the presence of labor market imperfections Xavier Pautrel

18-8. Identity mistakes and the standard of proof Marie Obidzinski, Yves Oytana

18-7. Presumption of innocence and deterrence Marie Obidzinski, Yves Oytana

18-6. Ethnic Discrimination in Rental Housing Market: An Experiment in New Caledonia Mathieu Bunel, Samuel Gorohouna, Yannick L'Horty, Pascale Petit, Catherine Ris

18-5. Evaluating the impact of firm tax credits. Results from the French natural experiment CICE

Fabrice Gilles, Yannick L'Horty, Ferhat Mihoubi, Xi Yang

18-4. Impact of type 2 diabetes on health expenditure: an estimation based on individual administrative data

François-Olivier Baudot , Anne-Sophie Aguadé, Thomas Barnay, Christelle Gastaldi-Ménager, Anne Fargot-Campagna

18-3. How does labour market history influence the access to hiring interviews? Emmanuel Duguet, Rémi Le Gall, Yannick L'Horty, Pascale Petit

18-2. Occupational mobility and vocational training over the life cycle Anthony Terriau

18-1. Retired, at last? The short-term impact of retirement on health status in France Thomas Barnay, Eric Defebvre

17-11. Hiring discrimination against women: distinguishing taste based discrimination from statistical discrimination

Emmanuel Duguet, Loïc du Parquet, Pascale Petit

17-10. Pension reforms, older workers' employment and the role of job separation and finding rates in France

Sarah Le Duigou, Pierre-Jean Messe

17-9. Healthier when retiring earlier? Evidence from France Pierre-Jean Messe, François-Charles Wolff

17-8. Revisting Hopenhayn and Nicolini's optimal unemployment insurance with job search monitoring and sanctions

Sebastien Menard, Solenne Tanguy

17-7. Ethnic Gaps in Educational Attainment and Labor-Market Outcomes: Evidence from France

Gabin Langevin, David Masclet, Fabien Moizeau, Emmanuel Peterle

17-6. Identifying preference-based discrimination in rental market: a field experiment in Paris

Mathieu Bunel, Yannick L'Horty, Loïc du Parquet, Pascale Petit

17-5. Chosen or Imposed? The location strategies of households Emilie Arnoult, Florent Sari

17-4. Optimal income taxation with composition effects

Laurence Jacquet, Etienne Lehmann

17-3. Labor Market Effects of Urban Riots: an experimental assessment Emmanuel Duguet, David Gray, Yannick L'Horty, Loic du Parquet, Pascale Petit

17-2. Does practicing literacy skills improve academic performance in first-year university students? Results from a randomized experiment Estelle Bellity, Fabrices Gilles, Yannick L'Horty

17-1. Raising the take-up of social assistance benefits through a simple mailing: evidence from a French field experiment

Sylvain Chareyron, David Gray, Yannick L'Horty

16-8. Endogenous wage rigidities, human capital accumulation and growth Ahmed Tritah

16-7. Harder, better, faster...yet stronger? Working conditions and self-declaration of chronic diseases Eric Defebvre

Life Deleuvie

16-6. The influence of mental health on job retention Thomas Barnay, Eric Defebvre

16-5. The effects of breast cancer on individual labour market outcomes: an evaluation from an administrative panel

Thomas Barnay, Mohamed Ali Ben Halima, Emmanuel Duguet, Christine Le Clainche, Camille Regaert

16-4. Expectations, Loss Aversion, and Retirement Decisions in the Context of the 2009 Crisis in Europe

Nicolas Sirven, Thomas Barnay

16-3. How do product and labor market regulations affect aggregate employment, inequalities and job polarization? A general equilibrium approach

Julien Albertini, Jean-Olivier Hairault, François Langot, Thepthida Sopraseuth

16-2. Access to employment with age and gender: results of a controlled experiment Laetitia Challe, Florent Fremigacci, François Langot, Yannick L'Horty, Loïc Du Parquet, Pascale Petit

16-1. An evaluation of the 1987 French Disabled Workers Act: Better paying than hiring Thomas Barnay, Emmanuel Duguet, Christine Le Clainche, Yann Videau

15-10. Optimal Income Taxation with Unemployment and Wage Responses: A Sufficient Statistics Approach

Kory Kroft, Kavan Kucko, Etienne Lehmann, Johannes Schmieder

15-9. Search frictions and (in) efficient vocational training over the life-cycle Arnaud Chéron, Anthony Terriau

15-8. Absenteeism and productivity: the experience rating applied to employer contributions to health insurance

Sébastien Ménard, Coralia Quintero Rojas

15-7. Take up of social assistance benefits: the case of homeless Sylvain Chareyron

15-6. Spatial mismatch through local public employment agencies. Answers from a French quasi-experiment

Mathieu Bunel, Elisabeth Tovar

15-5. Transmission of vocational skills at the end of career: horizon effect and technological or organisational change

Nathalie Greenan, Pierre-Jean Messe

15-4. Protecting biodiversity by developing bio-jobs: A multi-branch analysis with an application on French data

Jean De Beir, Céline Emond, Yannick L'Horty, Laetitia Tuffery

15-3. Profit-Sharing and Wages: An Empirical Analysis Using French Data Between 2000 and 2007

Noélie Delahaie, Richard Duhautois

15-2. A meta-regression analysis on intergenerational transmission of education: publication bias and genuine empirical effect Nicolas Eleury, Eabrice Gilles

Nicolas Fleury, Fabrice Gilles

15-1. Why are there so many long-term unemployed in Paris?

Yannick L'Horty, Florent Sari

14-14. Hiring discrimination based on national origin and the competition between employed and unemployed job seekers

Guillaume Pierné

14-13. Discrimination in Hiring: The curse of motorcycle women Loïc Du Parquet, Emmanuel Duguet, Yannick L'Horty, Pascale Petit

14-12. Residential discrimination and the ethnic origin: An experimental assessment in the Paris suburbs

Emmanuel Duguet, Yannick L'Horty, Pascale Petit

14-11. Discrimination based on place of residence and access to employment Mathieu Bunel, Yannick L'Horty, Pascale Petit

14-10. Rural Electrification and Household Labor Supply: Evidence from Nigeria Claire Salmon, Jeremy Tanguy

14-9. Effects of immigration in frictional labor markets: theory and empirical evidence from EU countries

Eva Moreno-Galbis, Ahmed Tritah

14-8. Health, Work and Working Conditions: A Review of the European Economic Literature Thomas Barnay

14-7. Labour mobility and the informal sector in Algeria: a cross-sectional comparison (2007-2012)

Philippe Adair, Youghourta Bellache

14-6. Does care to dependent elderly people living at home increase their mental health? Thomas Barnay, Sandrine Juin

14-5. The Effect of Non-Work Related Health Events on Career Outcomes: An Evaluation in the French Labor Market

Emmanuel Duguet, Christine le Clainche

14-4. Retirement intentions in the presence of technological change: Theory and evidence from France

Pierre-Jean Messe, Eva Moreno-Galbis, Francois-Charles Wolff

14-3. Why is Old Workers' Labor Market more Volatile? Unemployment Fluctuations over the Life-Cycle

Jean-Olivier Hairault, François Langot, Thepthida Sopraseuth

14-2. Participation, Recruitment Selection, and the Minimum Wage Frédéric Gavrel

14-1. Disparities in taking sick leave between sectors of activity in France: a longitudinal analysis of administrative data

Thomas Barnay, Sandrine Juin, Renaud Legal

13-9. An evaluation of the impact of industrial restructuring on individual human capital accumulation in France (1956-1993)

Nicolas Fleury, Fabrice Gilles

13-8. On the value of partial commitment for cooperative investment in buyer-supplier relationship

José de Sousa, Xavier Fairise

13-7. Search frictions, real wage rigidities and the optimal design of unemployment insurance Julien Albertini, Xavier Fairise

13-6. Tax me if you can! Optimal nonlinear income tax between competing governments Etienne Lehmann, Laurent Simula, Alain Trannoy

13-5. Beyond the labour income tax wedge: The unemployment-reducing effect of tax progressivity

Etienne Lehmann, Claudio Lucifora, Simone Moriconi, Bruno Van Der Linden

13-4. Discrimination based on place of residence and access to employment Mathieu Bunel, Emilia Ene Jones, Yannick L'Horty, Pascale Petit

13-3. The determinants of job access channels: evidence from the youth labor market in France Jihan Ghrairi

13-2. Capital mobility, search unemployment and labor market policies: The case of minimum wages

Frédéric Gavrel

13-1. Effort and monetary incentives in Nonprofit et For-Profit Organizations Joseph Lanfranchi, Mathieu Narcy

The TEPP Institute

The CNRS **Institute for Theory and Evaluation of Public Policies** (the TEPP Institute, FR n°2024 CNRS) gathers together research centres specializing in economics and sociology:

- L'Equipe de Recherche sur l'Utilisation des Données Individuelles en lien avec la Théorie Economique (Research Team on Use of Individuals Data in connection with economic theory), ERUDITE, University of Paris-Est Créteil and University of Gustave Eiffel
- Le Centre d'Etudes des Politiques Economiques de l'université d'Evry (Research Centre focused on the analysis of economic policy and its foundations and implications), EPEE, University of Evry Val d'Essonne
- Le Centre Pierre Naville (Research on Work and Urban Policies), CPN, University of Evry Val d'Essonne
- Le Groupe d'Analyse des Itinéraires et des Niveaux Salariaux (Group on Analysis of Wage Levels and Trajectories), GAINS, University of Le Mans
- Le Centre de Recherches en Economie et en Management, (Research centre in Economics and Management), CREM, University of Rennes 1 et University of Caen Basse-Normandie
- Le Groupe de Recherche ANgevin en Économie et Management (Angevin Research Group in Economics and Management), GRANEM, University of Angers
- Le Centre de Recherche en Economie et Droit (Research centre in Economics and Law)
 CRED, University of Paris II Panthéon-Assas
- Le Laboratoire d'Economie et de Management Nantes-Atlantique (Laboratory of Economics and Management of Nantes-Atlantique) LEMNA, University of Nantes
- Le Laboratoire interdisciplinaire d'étude du politique Hannah Arendt Paris Est, LIPHA-PE
- Le Centre d'Economie et de Management de l'Océan Indien, CEMOI, University of La Réunion

TEPP brings together 230 teacher-researchers and 100 doctoral students. It is both one of the main academic operators in the evaluation of public policies in France, and the largest multidisciplinary federation of research on work and employment. It responds to the demand for impact assessment of social programs using advanced technologies combining theoretical and econometric modeling, qualitative research techniques and controlled experiences.

www.tepp.eu